

WHAT IS AN EXTREMA IN MATH

WHAT IS AN EXTREMA IN MATH: A COMPREHENSIVE GUIDE

WHAT IS AN EXTREMA IN MATH REFERS TO THE HIGHEST OR LOWEST POINTS OF A FUNCTION'S GRAPH. THESE CRITICAL VALUES, OFTEN CALLED MAXIMA AND MINIMA, ARE FUNDAMENTAL TO UNDERSTANDING THE BEHAVIOR AND CHARACTERISTICS OF MATHEMATICAL FUNCTIONS. WHETHER YOU'RE EXPLORING CALCULUS, OPTIMIZATION PROBLEMS, OR SIMPLY TRYING TO VISUALIZE A CURVE, IDENTIFYING EXTREMA PROVIDES CRUCIAL INSIGHTS INTO WHERE A FUNCTION REACHES ITS PEAK PERFORMANCE OR ITS LOWEST EBB. THIS ARTICLE WILL DELVE INTO THE DEFINITIONS, TYPES, AND METHODS FOR FINDING THESE SIGNIFICANT POINTS, COVERING BOTH LOCAL AND GLOBAL EXTREMA AND THEIR APPLICATIONS ACROSS VARIOUS MATHEMATICAL DISCIPLINES. WE'LL BREAK DOWN THE CONCEPTS OF CRITICAL POINTS, DERIVATIVES, AND THE SECOND DERIVATIVE TEST, EMPOWERING YOU TO CONFIDENTLY ANALYZE AND INTERPRET THE EXTREMAL VALUES OF ANY GIVEN FUNCTION.

TABLE OF CONTENTS

UNDERSTANDING THE CONCEPT OF EXTREMA

TYPES OF EXTREMA: LOCAL VS. GLOBAL

FINDING EXTREMA: THE ROLE OF CALCULUS

CRITICAL POINTS: THE STARTING POINT FOR FINDING EXTREMA

THE FIRST DERIVATIVE TEST FOR EXTREMA

THE SECOND DERIVATIVE TEST FOR EXTREMA

EXTREMA IN REAL-WORLD APPLICATIONS

PRACTICAL EXAMPLES OF EXTREMA IN MATH

UNDERSTANDING THE CONCEPT OF EXTREMA

AT ITS CORE, AN EXTREMUM IN MATHEMATICS REPRESENTS A POINT WHERE A FUNCTION ATTAINS ITS MAXIMUM OR MINIMUM VALUE. THINK OF IT AS THE SUMMIT OF A MOUNTAIN OR THE BOTTOM OF A VALLEY ON A TOPOGRAPHICAL MAP. THESE POINTS ARE INCREDIBLY IMPORTANT BECAUSE THEY OFTEN SIGNIFY A CHANGE IN THE FUNCTION'S BEHAVIOR. FOR A FUNCTION OF A SINGLE VARIABLE, SAY $f(x)$, AN EXTREMUM OCCURS AT A SPECIFIC x -VALUE, AND THE CORRESPONDING y -VALUE, $f(x)$, IS THE EXTREMUM VALUE. THIS CONCEPT ISN'T LIMITED TO SIMPLE CURVES; IT EXTENDS TO FUNCTIONS WITH MULTIPLE VARIABLES, WHERE WE LOOK FOR HIGHEST AND LOWEST POINTS IN HIGHER DIMENSIONS.

THE TERM "EXTREMA" IS ACTUALLY THE PLURAL FORM; A SINGLE HIGHEST OR LOWEST POINT IS CALLED AN "EXTREMUM." WHEN WE TALK ABOUT BOTH THE HIGHEST AND LOWEST POINTS TOGETHER, WE USE THE COLLECTIVE TERM "EXTREMA."

UNDERSTANDING THESE POINTS HELPS US GRASP THE OVERALL SHAPE AND TRENDS OF A FUNCTION, ALLOWING US TO PREDICT ITS BEHAVIOR AND SOLVE COMPLEX PROBLEMS IN FIELDS LIKE PHYSICS, ECONOMICS, AND ENGINEERING. WITHOUT IDENTIFYING EXTREMA, OUR UNDERSTANDING OF A FUNCTION WOULD BE INCOMPLETE, LIKE TRYING TO NAVIGATE A LANDSCAPE WITHOUT KNOWING ITS PEAKS AND TROUGHS.

TYPES OF EXTREMA: LOCAL VS. GLOBAL

WHEN DISCUSSING EXTREMA, IT'S CRUCIAL TO DIFFERENTIATE BETWEEN TWO MAIN TYPES: LOCAL EXTREMA AND GLOBAL EXTREMA. THESE CLASSIFICATIONS HELP US PINPOINT THE SIGNIFICANCE OF A PARTICULAR MAXIMUM OR MINIMUM WITHIN A SPECIFIC REGION OR ACROSS THE ENTIRE DOMAIN OF A FUNCTION.

LOCAL EXTREMA: PEAKS AND VALLEYS IN A NEIGHBORHOOD

A LOCAL MAXIMUM OCCURS AT A POINT c IF $f(c) \geq f(x)$ FOR ALL x IN SOME OPEN INTERVAL CONTAINING c .

CONVERSELY, A LOCAL MINIMUM OCCURS AT A POINT c IF $f(c) \leq f(x)$ FOR ALL x IN SOME OPEN INTERVAL CONTAINING c . IMAGINE A ROLLER COASTER TRACK; THE VERY TOP OF A HILL IS A LOCAL MAXIMUM, AND THE BOTTOM OF A DIP IS A LOCAL MINIMUM. THESE POINTS ARE ONLY THE HIGHEST OR LOWEST WITHIN THEIR IMMEDIATE VICINITY, NOT NECESSARILY FOR THE ENTIRE RIDE.

IT'S IMPORTANT TO NOTE THAT A FUNCTION CAN HAVE MANY LOCAL MAXIMA AND LOCAL MINIMA. THESE ARE THE POINTS WHERE THE FUNCTION CHANGES DIRECTION FROM INCREASING TO DECREASING (FOR A LOCAL MAXIMUM) OR FROM DECREASING TO INCREASING (FOR A LOCAL MINIMUM). THEY ARE IDENTIFIED BY LOOKING FOR POINTS WHERE THE SLOPE OF THE TANGENT LINE IS ZERO OR UNDEFINED.

GLOBAL EXTREMA: THE ABSOLUTE HIGHEST AND LOWEST POINTS

GLOBAL EXTREMA, ALSO KNOWN AS ABSOLUTE EXTREMA, REPRESENT THE ABSOLUTE HIGHEST OR LOWEST VALUES OF A FUNCTION OVER ITS ENTIRE DOMAIN, OR A SPECIFIED INTERVAL. A GLOBAL MAXIMUM IS THE LARGEST VALUE THE FUNCTION EVER ACHIEVES, AND A GLOBAL MINIMUM IS THE SMALLEST VALUE IT EVER ACHIEVES. CONTINUING THE ROLLER COASTER ANALOGY, THE ABSOLUTE HIGHEST POINT OF THE ENTIRE TRACK WOULD BE THE GLOBAL MAXIMUM, AND THE ABSOLUTE LOWEST POINT WOULD BE THE GLOBAL MINIMUM. THESE ARE THE MOST EXTREME VALUES THE FUNCTION WILL EVER TAKE.

FOR A CONTINUOUS FUNCTION ON A CLOSED INTERVAL, THE EXTREME VALUE THEOREM GUARANTEES THAT BOTH A GLOBAL MAXIMUM AND A GLOBAL MINIMUM EXIST. THESE GLOBAL EXTREMA CAN OCCUR AT EITHER THE ENDPOINTS OF THE INTERVAL OR AT CRITICAL POINTS WITHIN THE INTERVAL WHERE LOCAL EXTREMA MIGHT BE FOUND.

FINDING EXTREMA: THE ROLE OF CALCULUS

CALCULUS PROVIDES THE POWERFUL TOOLS NEEDED TO PRECISELY LOCATE AND IDENTIFY EXTREMA. THE FUNDAMENTAL CONCEPT BEHIND FINDING EXTREMA INVOLVES EXAMINING THE RATE OF CHANGE OF A FUNCTION, WHICH IS PRECISELY WHAT DERIVATIVES MEASURE. BY ANALYZING THE SLOPE OF THE TANGENT LINE TO THE FUNCTION'S GRAPH, WE CAN DETERMINE WHERE THE FUNCTION IS INCREASING, DECREASING, OR MOMENTARILY PAUSING AT A PEAK OR TROUGH.

THE DERIVATIVE OF A FUNCTION, $f'(x)$, TELLS US THE SLOPE OF THE TANGENT LINE AT ANY GIVEN POINT x . WHERE THE FUNCTION TRANSITIONS FROM INCREASING TO DECREASING, THE DERIVATIVE OFTEN CHANGES FROM POSITIVE TO NEGATIVE, PASSING THROUGH ZERO. SIMILARLY, WHERE IT TRANSITIONS FROM DECREASING TO INCREASING, THE DERIVATIVE TYPICALLY CHANGES FROM NEGATIVE TO POSITIVE, AGAIN, OFTEN PASSING THROUGH ZERO. THESE POINTS WHERE THE DERIVATIVE IS ZERO OR UNDEFINED ARE OUR PRIMARY CANDIDATES FOR EXTREMA.

CRITICAL POINTS: THE STARTING POINT FOR FINDING EXTREMA

CRITICAL POINTS ARE THE LINCHPINS IN OUR QUEST TO FIND EXTREMA. A CRITICAL POINT OF A FUNCTION $f(x)$ IS ANY POINT c IN THE DOMAIN OF f WHERE EITHER $f'(c) = 0$ OR $f'(c)$ IS UNDEFINED. THESE ARE THE ONLY LOCATIONS WHERE LOCAL EXTREMA CAN OCCUR. THINK OF THEM AS POTENTIAL TURNING POINTS ON THE GRAPH OF A FUNCTION. IF A FUNCTION HAS A SMOOTH, CONTINUOUS CURVE, THE CRITICAL POINTS ARE TYPICALLY WHERE THE TANGENT LINE IS HORIZONTAL (SLOPE IS ZERO).

HOWEVER, WE MUST ALSO CONSIDER POINTS WHERE THE DERIVATIVE IS UNDEFINED. THESE CAN OCCUR AT SHARP CORNERS OR CUSPS IN THE GRAPH. FOR INSTANCE, THE ABSOLUTE VALUE FUNCTION, $f(x) = |x|$, HAS A SHARP CORNER AT $x = 0$. ITS DERIVATIVE IS UNDEFINED AT THIS POINT, AND INDEED, $x = 0$ IS A LOCAL AND GLOBAL MINIMUM FOR THIS FUNCTION. THEREFORE, WHEN SEARCHING FOR EXTREMA, OUR FIRST STEP IS ALWAYS TO IDENTIFY ALL CRITICAL POINTS.

THE PROCESS OF FINDING CRITICAL POINTS INVOLVES:

- FINDING THE FIRST DERIVATIVE OF THE FUNCTION, $f'(x)$.
- SETTING THE DERIVATIVE EQUAL TO ZERO AND SOLVING FOR x TO FIND WHERE $f'(x) = 0$.
- IDENTIFYING ANY VALUES OF x FOR WHICH $f'(x)$ IS UNDEFINED.

THESE VALUES OF x , ALONG WITH ANY ENDPOINTS OF A SPECIFIED INTERVAL, BECOME THE CANDIDATES FOR EXTREMA.

THE FIRST DERIVATIVE TEST FOR EXTREMA

ONCE WE'VE IDENTIFIED THE CRITICAL POINTS, THE FIRST DERIVATIVE TEST IS A STRAIGHTFORWARD METHOD TO DETERMINE WHETHER EACH CRITICAL POINT CORRESPONDS TO A LOCAL MAXIMUM, A LOCAL MINIMUM, OR NEITHER. THIS TEST RELIES ON OBSERVING THE SIGN CHANGES IN THE FIRST DERIVATIVE AROUND THE CRITICAL POINT. ESSENTIALLY, WE'RE CHECKING IF THE FUNCTION IS INCREASING OR DECREASING ON EITHER SIDE OF THE CRITICAL POINT.

HERE'S HOW IT WORKS:

- **FOR A LOCAL MAXIMUM:** IF $f'(x)$ CHANGES FROM POSITIVE TO NEGATIVE AS x INCREASES THROUGH A CRITICAL POINT c , THEN $f(c)$ IS A LOCAL MAXIMUM. THIS MEANS THE FUNCTION WAS INCREASING BEFORE c AND STARTED DECREASING AFTER c .
- **FOR A LOCAL MINIMUM:** IF $f'(x)$ CHANGES FROM NEGATIVE TO POSITIVE AS x INCREASES THROUGH A CRITICAL POINT c , THEN $f(c)$ IS A LOCAL MINIMUM. THIS INDICATES THE FUNCTION WAS DECREASING BEFORE c AND BEGAN INCREASING AFTER c .
- **FOR NEITHER:** IF $f'(x)$ DOES NOT CHANGE SIGN AS x INCREASES THROUGH c (I.E., IT'S POSITIVE ON BOTH SIDES OR NEGATIVE ON BOTH SIDES), THEN $f(c)$ IS NEITHER A LOCAL MAXIMUM NOR A LOCAL MINIMUM. THIS OFTEN HAPPENS AT AN INFLECTION POINT WHERE THE CONCAVITY CHANGES.

TO APPLY THIS TEST, WE SELECT TEST VALUES IN THE INTERVALS DEFINED BY THE CRITICAL POINTS AND ENDPOINTS, AND EVALUATE THE SIGN OF $f'(x)$ AT THESE TEST VALUES. THE PATTERN OF SIGNS WILL REVEAL THE NATURE OF THE EXTREMA.

THE SECOND DERIVATIVE TEST FOR EXTREMA

ANOTHER POWERFUL TOOL FOR CLASSIFYING CRITICAL POINTS IS THE SECOND DERIVATIVE TEST. THIS METHOD USES THE SECOND DERIVATIVE OF A FUNCTION, $f''(x)$, TO DETERMINE CONCAVITY AT A CRITICAL POINT. THE CONCAVITY OF THE FUNCTION'S GRAPH AT A CRITICAL POINT CAN TELL US WHETHER IT'S A MAXIMUM OR MINIMUM.

THE TEST IS AS FOLLOWS:

- IF $f'(c) = 0$ AND $f''(c) < 0$, THEN $f(c)$ IS A LOCAL MAXIMUM. A NEGATIVE SECOND DERIVATIVE INDICATES THAT THE FUNCTION IS CONCAVE DOWN AT c , LIKE AN UPSIDE-DOWN BOWL, MEANING THE POINT IS A PEAK.
- IF $f'(c) = 0$ AND $f''(c) > 0$, THEN $f(c)$ IS A LOCAL MINIMUM. A POSITIVE SECOND DERIVATIVE SIGNIFIES THAT THE FUNCTION IS CONCAVE UP AT c , LIKE A RIGHT-SIDE-UP BOWL, MEANING THE POINT IS A TROUGH.
- IF $f'(c) = 0$ AND $f''(c) = 0$, THE TEST IS INCONCLUSIVE. IN SUCH CASES, WE MUST REVERT TO THE FIRST DERIVATIVE TEST TO DETERMINE THE NATURE OF THE CRITICAL POINT.

THE SECOND DERIVATIVE TEST IS OFTEN QUICKER THAN THE FIRST DERIVATIVE TEST, ESPECIALLY FOR FUNCTIONS WHERE CALCULATING THE SECOND DERIVATIVE IS EASY. HOWEVER, IT ONLY APPLIES TO CRITICAL POINTS WHERE THE FIRST DERIVATIVE IS ZERO, NOT WHERE IT IS UNDEFINED.

EXTREMA IN REAL-WORLD APPLICATIONS

THE CONCEPT OF EXTREMA IS FAR FROM BEING JUST AN ABSTRACT MATHEMATICAL IDEA; IT HAS PROFOUND IMPLICATIONS AND WIDESPREAD APPLICATIONS IN SOLVING REAL-WORLD PROBLEMS. WHENEVER WE SEEK TO OPTIMIZE A SITUATION – TO FIND THE BEST POSSIBLE OUTCOME, WHETHER IT'S MAXIMIZING PROFIT, MINIMIZING COST, OR ACHIEVING PEAK EFFICIENCY – WE ARE ESSENTIALLY LOOKING FOR EXTREMA.

CONSIDER A BUSINESS OWNER WHO WANTS TO MAXIMIZE THEIR PROFIT. THEY MIGHT USE A FUNCTION THAT MODELS PROFIT BASED ON PRODUCTION LEVELS. FINDING THE MAXIMUM VALUE OF THIS PROFIT FUNCTION WILL TELL THEM THE OPTIMAL NUMBER OF UNITS TO PRODUCE TO ACHIEVE THE HIGHEST POSSIBLE EARNINGS. SIMILARLY, AN ENGINEER DESIGNING A BRIDGE MIGHT NEED TO MINIMIZE THE AMOUNT OF MATERIAL USED WHILE ENSURING STRUCTURAL INTEGRITY. THIS INVOLVES FINDING THE MINIMUM VALUE OF A COST FUNCTION, WHICH IN TURN MINIMIZES THE MATERIAL REQUIRED.

IN PHYSICS, EXTREMA ARE CRUCIAL FOR UNDERSTANDING TRAJECTORIES, ENERGY LEVELS, AND FORCES. FOR INSTANCE, THE MAXIMUM HEIGHT REACHED BY A PROJECTILE IS A GLOBAL MAXIMUM OF ITS VERTICAL POSITION FUNCTION. IN ECONOMICS, CONCEPTS LIKE MARGINAL COST AND MARGINAL REVENUE OFTEN INVOLVE FINDING POINTS OF MINIMUM OR MAXIMUM VALUE TO UNDERSTAND ECONOMIC EFFICIENCIES AND OPTIMAL PRICING STRATEGIES.

PRACTICAL EXAMPLES OF EXTREMA IN MATH

LET'S CONSIDER A SIMPLE POLYNOMIAL FUNCTION TO ILLUSTRATE HOW WE FIND EXTREMA. SUPPOSE WE HAVE THE FUNCTION $f(x) = x^3 - 6x^2 + 5x$. TO FIND THE LOCAL EXTREMA:

1. **FIND THE FIRST DERIVATIVE:** $f'(x) = 3x^2 - 12x$.
2. **SET THE DERIVATIVE TO ZERO TO FIND CRITICAL POINTS:** $3x^2 - 12x = 0$ IMPLIES $3x(x - 4) = 0$. THIS GIVES US CRITICAL POINTS AT $x = 0$ AND $x = 4$.
3. **FIND THE SECOND DERIVATIVE:** $f''(x) = 6x - 12$.
4. **APPLY THE SECOND DERIVATIVE TEST:**
 - AT $x = 0$: $f''(0) = 6(0) - 12 = -12$. SINCE $f''(0) < 0$, $f(0)$ IS A LOCAL MAXIMUM.
 - AT $x = 4$: $f''(4) = 6(4) - 12 = 24 - 12 = 12$. SINCE $f''(4) > 0$, $f(4)$ IS A LOCAL MINIMUM.
5. **CALCULATE THE FUNCTION VALUES AT THESE POINTS:**
 - LOCAL MAXIMUM VALUE: $f(0) = 0^3 - 6(0)^2 + 5 = 5$. So, $(0, 5)$ IS A LOCAL MAXIMUM.
 - LOCAL MINIMUM VALUE: $f(4) = 4^3 - 6(4)^2 + 5 = 64 - 96 + 5 = -27$. So, $(4, -27)$ IS A LOCAL MINIMUM.

THIS EXAMPLE DEMONSTRATES THE SYSTEMATIC APPROACH TO IDENTIFYING EXTREMA USING CALCULUS. BY UNDERSTANDING THESE POINTS, WE GAIN A COMPREHENSIVE PICTURE OF THE FUNCTION'S BEHAVIOR, FROM ITS HIGHEST PEAKS TO ITS LOWEST VALLEYS.

FAQ SECTION

Q: WHAT IS THE BASIC DEFINITION OF AN EXTREMUM IN MATHEMATICS?

A: AN EXTREMUM IN MATHEMATICS REFERS TO A POINT WHERE A FUNCTION ATTAINS ITS MAXIMUM OR MINIMUM VALUE. THESE POINTS CAN BE EITHER LOCAL, MEANING THEY ARE THE HIGHEST OR LOWEST IN A SPECIFIC NEIGHBORHOOD, OR GLOBAL, MEANING THEY ARE THE ABSOLUTE HIGHEST OR LOWEST VALUES ACROSS THE ENTIRE DOMAIN OF THE FUNCTION.

Q: HOW ARE LOCAL EXTREMA DIFFERENT FROM GLOBAL EXTREMA?

A: LOCAL EXTREMA ARE POINTS THAT ARE EITHER A MAXIMUM OR MINIMUM WITHIN A SMALL, SURROUNDING INTERVAL OF THE FUNCTION'S GRAPH. THEY REPRESENT PEAKS OR VALLEYS IN A LIMITED REGION. GLOBAL EXTREMA, ON THE OTHER HAND, ARE THE ABSOLUTE HIGHEST OR LOWEST VALUES THE FUNCTION REACHES OVER ITS ENTIRE DOMAIN OR A SPECIFIED INTERVAL. A FUNCTION CAN HAVE MULTIPLE LOCAL EXTREMA BUT TYPICALLY ONLY ONE GLOBAL MAXIMUM AND ONE GLOBAL MINIMUM VALUE (THOUGH THEY MAY OCCUR AT MULTIPLE POINTS).

Q: WHAT ARE CRITICAL POINTS, AND WHY ARE THEY IMPORTANT FOR FINDING EXTREMA?

A: CRITICAL POINTS ARE POINTS IN THE DOMAIN OF A FUNCTION WHERE THE FIRST DERIVATIVE IS EITHER EQUAL TO ZERO OR UNDEFINED. THESE ARE THE ONLY POTENTIAL LOCATIONS FOR LOCAL EXTREMA TO OCCUR. BY IDENTIFYING CRITICAL POINTS, WE NARROW DOWN THE SEARCH FOR MAXIMUM AND MINIMUM VALUES TO A MANAGEABLE SET OF CANDIDATES.

Q: CAN A FUNCTION HAVE AN EXTREMUM WHERE ITS DERIVATIVE IS UNDEFINED?

A: YES, A FUNCTION CAN HAVE AN EXTREMUM WHERE ITS DERIVATIVE IS UNDEFINED. THIS TYPICALLY OCCURS AT SHARP CORNERS OR CUSPS IN THE GRAPH OF THE FUNCTION. THE ABSOLUTE VALUE FUNCTION, $f(x)=|x|$, IS A CLASSIC EXAMPLE WHERE THE MINIMUM AT $x=0$ OCCURS WHERE THE DERIVATIVE IS UNDEFINED.

Q: WHAT IS THE ROLE OF THE FIRST DERIVATIVE IN FINDING EXTREMA?

A: THE FIRST DERIVATIVE, $f'(x)$, TELLS US THE SLOPE OF THE TANGENT LINE TO THE FUNCTION'S GRAPH. BY EXAMINING THE SIGN CHANGES OF THE FIRST DERIVATIVE AROUND A CRITICAL POINT, WE CAN DETERMINE IF THE FUNCTION IS INCREASING OR DECREASING BEFORE AND AFTER THAT POINT. A CHANGE FROM INCREASING TO DECREASING INDICATES A LOCAL MAXIMUM, AND A CHANGE FROM DECREASING TO INCREASING INDICATES A LOCAL MINIMUM.

Q: HOW DOES THE SECOND DERIVATIVE TEST HELP IN CLASSIFYING EXTREMA?

A: THE SECOND DERIVATIVE TEST USES THE CONCAVITY OF THE FUNCTION AT A CRITICAL POINT WHERE THE FIRST DERIVATIVE IS ZERO. IF THE SECOND DERIVATIVE IS NEGATIVE, THE FUNCTION IS CONCAVE DOWN, INDICATING A LOCAL MAXIMUM. IF THE SECOND DERIVATIVE IS POSITIVE, THE FUNCTION IS CONCAVE UP, INDICATING A LOCAL MINIMUM. IF THE SECOND DERIVATIVE IS ZERO, THE TEST IS INCONCLUSIVE, AND THE FIRST DERIVATIVE TEST MUST BE USED.

Q: ARE EXTREMA ONLY RELEVANT IN THEORETICAL MATHEMATICS, OR DO THEY HAVE

PRACTICAL APPLICATIONS?

A: EXTREMA ARE INCREDIBLY RELEVANT IN PRACTICAL APPLICATIONS. THEY ARE USED IN OPTIMIZATION PROBLEMS ACROSS VARIOUS FIELDS, SUCH AS ECONOMICS (MAXIMIZING PROFIT, MINIMIZING COST), ENGINEERING (OPTIMIZING DESIGNS), PHYSICS (FINDING MAXIMUM HEIGHTS OR MINIMUM ENERGIES), AND OPERATIONS RESEARCH (FINDING THE MOST EFFICIENT SOLUTIONS).

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